****

**MATHEMATICS  
METHODS**

**Sequences and Series**

**Semester 2 2023**

# 

**Section Two – Calculator Assumed**

Time allowed for this section

Working time for this section: 35 minutes

Marks available: 37 marks

## Material required/recommended for this section

##### To be provided by the supervisor

This Question/Answer booklet

Formula sheet

##### To be provided by the candidate

Standard items: pens, pencils, pencil sharpener, eraser, correction fluid, ruler, highlighters

Special items: drawing instruments, templates, notes on one unfolded sheet of A4 paper, and up to three calculators satisfying the conditions set by the Curriculum Council for this course.

## Important note to candidates

No other items may be used in this section of the examination. It is **your** responsibility to ensure that you do not have any unauthorised notes or other items of a non-personal nature in the examination room. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

1. (9 marks)  
   The first term of an arithmetic sequence is 2 and the 5th term is 14.
2. Determine the common difference of this sequence. [2]
3. Hence or otherwise define this sequence recursively. [2]
4. Calculate T10 [1]
5. Calculate S10  [2]
6. Determine when the sequence first has a value greater than 100. [2]
7. (5 marks)

Eighty students participate in a fundraising event for charity. The student who raises the most money is rewarded with an $80 credit to spend at the canteen. The student who raises the second largest amount receives a $79 credit and this continues with the person who raises the least receiving just a $1 credit.

1. How much money is needed to give each of the 80 students their reward? [2]
2. How much money is needed to give each of the bottom 20 students their reward? [2]
3. [5 marks]

The fourth term of a geometric sequence is 3125 and the sum of the 5th, 6th and 7th terms is 76171.875.

Determine a recursive rule for this geometric sequence.

1. (11 marks)

Winona is training for a half marathon. Her goal is to be able to run the full 21 km in 100 minutes.

On her first run she completes the half marathon in 150 minutes. On her second run it takes her 148 minutes to complete the 21 km, and on the third run it takes her 146 minutes. Her run times continue in this way.

1. How long will it take her to run the half marathon on her 10th training session? [2]
2. How long will it take her to run the half marathon on her nth training session? [2]
3. When will she be able to run the half marathon in less than 2 hours? [2]
4. How long has she spent training during her first seven runs? [2]
5. If her training continues in this way, when will she achieve her goal? [1]
6. Winona wonders if her training can reap these sort of results indefinitely. [2] Explain whether Winona can keep achieving these results.
7. (7 marks)

A ball is dropped from a height of 3 m. On each bounce back up the ball reaches a height 80% of its previous height.

1. Determine the height reached on the first bounce. [1]
2. Write a recursive rule defining the height of each bounce after the first bounce. [2]
3. Calculate the total vertical distance travelled by the ball after 10 bounces. [2]
4. If the ball bounces indefinitely, calculate the total vertical distance travelled. [2]

**End of Test**